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## **THE PRACTICAL ASPECT OF USING A COMBINATORIAL MODEL ON CONFIGURATION OF COMBINATIONS**

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*The paper proposes the practical task of choosing a set of programs to protect information at the enterprise. An optimization combinatorial model is built on the configuration of combinations to solve the task. An algorithm for finding a solution to this optimization problem is presented. A practical example of the use of a optimization combinatorial model and the search for the best choice of a set of programs for data protection at the enterprise is given.*

**Keywords:** *information security, combinatorial optimization, mathematical model, a configuration of combinations, objective function, restrictions.*

### **Introduction**

Currently, the information security of an enterprise is one of the leading factors in its effective development. The information has a real value weight, which is clearly determined by the profit received during its use, or the damage that may be caused to an enterprise if it is used by other persons [1–2]. The share of organizations' expenses on ensuring the integrity of information and protecting it from possible external threats is constantly growing. However, the profitability of the enterprise depends on the profit and costs spent on making a profit. Therefore, enterprises are trying to optimize costs, and they want to buy only what is really necessary to build a reliable information protection system with minimal costs [3].

Various aspects of data protection and the use of various methods based on cryptography are described in [4–6].

An integrated information security system at an enterprise provides for the solution of a number of tasks that give a solution to security problems at the software, hardware and organizational levels [7, 8]. From a practical point of view, the software level of protection is the most strategically important. The market for data security software is very diverse. For reliable protection of information at the enterprise, it is necessary to have several programs in a package that should provide needed protection in terms of identifying destabilizing factors and successfully preventing various types of threats. At the same time, it should be noted that comprehensive software packages for data protec-

tion have a high cost, therefore it is necessary to be able to make the best choice from the provided software, taking into account the necessary conditions that form the basic principles of information security in an enterprise.

When modelling various processes and phenomena in various fields of activity, models are often used, which are presented as tasks of conditional optimization. Particularly noteworthy are the models of such problems considered on combinatorial sets. To date, a significant amount of work has been devoted to the study and investigation of models of combinatorial nature [9–10].

Despite the simplicity of constructing combinatorial sets, combinatorial optimization problems are complex and time-consuming from a computational point of view [11–12], so there is a need to develop new methods and algorithms for solving them.

## Formulation of the Problem

In the software market, there are many software products to protect information. There is no need to purchase large quantities, but you need to make an effective choice that ensures the prevention of threats and minimal losses during unauthorized intrusions. It should be noted that the price policy in the software market plays the same important role when choosing.

Therefore, coming out of the main tasks of data protection and financial capabilities, as a rule, an enterprise needs to make a choice from the existing availability of programs of this type. It should be noted that data protection programs have a fairly wide range of overlapping functionalities. At the

same time, vary significantly in price and implementation requirements.

Each program has a rating in a general database of programs for certain functions. For example, ratings of antivirus programs can be found on certain sites taking into account the assessment of the main characteristics, such as threat detection, performance, false positives and others.

For ease of presentation, we assume that 1 is the program with the lowest rating, respectively,  $n$  – with the highest rating. The main task is to choose a set of programs with the highest rating taking into account the conditions of an enterprise. We assume that the average statistical prices for programs of the corresponding rating are known, then the choice should provide for minimal costs for acquiring the programs with the highest rating.

Since this set of programs should ensure the protection of information of the enterprise as a whole, it is natural to assume that each structural unit of the enterprise has its requirements for data protection software. Programs may coincide or differ, which mathematically can be formulated as a system of inequalities.

It is necessary to choose a set of programs that should have the highest rating possible and satisfy the conditions of the structural units of the enterprise. The choice of such programs should ensure the minimization of the costs of their acquisition. When detailing the choice, it is possible to perform additional calculations of the objective function in the range of maximum and minimum average prices of data protection programs, taking into account their rating.

## Combination Optimization Model

Let suppose that in the software market for an enterprise in a certain industry, information protection  $n$  programs that have their own specific rating  $A = (a_1, a_2, \dots, a_n)$ , ( $n \in N$ ). Having conducted a comprehensive assessment to identify destabilizing factors and possible losses from the invasion, taking into account the financial activities of the enterprise, it was found that there is a need to purchase  $k$  from  $n$  programs for the comprehensive protection of information.

Table 1. Price range of programs depending on rating

Rating of Programs	Price, \$	
	$p_1$	$p_2$
$a_1 = 1$	$c_{11}$	$c_{12}$
$a_2 = 2$	$c_{21}$	$c_{22}$
$a_3 = 3$	$c_{31}$	$c_{32}$
...	...	...
$a_n = n$	$c_{n1}$	$c_{n2}$





For the point (1, 2, 6):  $g_1 = 28 \geq 20$ ,  $g_2 = 10 > 5$  constraint is not satisfied.

For the point (1, 3, 4):  $g_1 = 27 \geq 20$ ,  $g_2 = 1 \leq 5$ ,  $g_3 = 38 < 43$  constraint is not satisfied.

For the point (1, 3, 5):  $g_1 = 31 \geq 20$ ,  $g_2 = 3 \leq 5$ ,  $g_3 = 44 \geq 43$  constraints are satisfied,  $F(135) = 62400$ . Accordingly, the first supporting solution is found. Then the initial search conditions for the next supporting solution:

$$\begin{cases} \Delta g_1 \geq -11, \\ \Delta g_2 \leq 2, \\ \Delta g_3 \geq -1. \end{cases}$$

Consider the next point (1, 3, 6):  $\Delta g_1 = 4 \geq -11$ ,  $\Delta g_2 = 2 \leq 2$ ,  $\Delta g_3 = 6 \geq -1$  constraints are satisfied, not  $\Delta F(136) = 22200$ . Therefore, this solution is not better than the previous one.

Therefore, point (1, 3, 5) is optimal solution. The minimum values of the objective function  $\min F(136) = \{62400 - 76200\}$ .

Answer: for comprehensive data protection, the enterprise «OZONINVEST» needs to purchase programs that have a 1st, 3th and 5th rating. The minimum cost of acquiring them will range from \$ 62400 to \$ 7600.

## Conclusion

The analysis of the problem of choosing a set of programs for protecting information at an enterprise of any industry is carried out. An optimization combinatorial model is constructed, taking into account the emerging conditions for the selection of data protection programs, as well as the financial activities of the enterprise. Using the bijective mapping of multiple combinations into Euclidean space, the mathematical model was considered on the configuration of combinations.

An algorithm for solving the problem, consisting of three steps. At the first and second steps, the search for the supporting solution was carried out, and the third step ensures the finding of the optimal solution. A numerical example of the implementation of the considered optimization combinatorial model on the set of configuration of combinations is given.

Further research is aimed at constructing mathematical models on other combinatorial configurations with nonlinear objective functions.

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## ПРАКТИЧНИЙ АСПЕКТ ЗАСТОСУВАННЯ КОМБІНАТОРНОЇ МОДЕЛІ НА КОНФІГУРАЦІЇ СПОЛУЧЕНЬ

**Вступ.** На ринку програмного забезпечення існує багато програмних продуктів щодо захисту інформації. Виходячи з основних завдань захисту інформації та фінансових можливостей, як правило, підприємству необхідно здійснювати вибір з наявності програм даного типу. Вибір таких програм має забезпечувати мінімізацію витрат на їх придбання. При деталізації вибору можна здійснити додаткові розрахунки цільової функції в діапазоні максимуму та мінімуму середньостатистичних цін програм захисту інформації з урахуванням їх рейтингу. При вирішенні даної проблеми є сенс використовувати комбінаторні оптимізаційні моделі на множині сполучень.

**Метою** даної статті є демонстрація використання комбінаторної оптимізаційної моделі на множині сполучень та подання методу вирішення даного типу завдань.

**Методи.** Метод розв'язання задачі умовної оптимізації на комбінаторній множині сполучень.

**Результати.** Сформульовано проблему вибору програмного забезпечення захисту інформації та запропоновано підхід до її розв'язання. В даному випадку завдання моделюється комбінаторною оптимізаційною моделлю на множині сполучень. Запропоновано метод розв'язання даного типу завдань. Розглянуто практичний приклад застосування комбінаторної оптимізаційної моделі на множині сполучень.

**Висновки.** За допомогою запропонованої моделі можна моделювати завдання, які передбачають сполучення об'єктів, процесів і т.п. за умови мінімізації функції мети. Подальші дослідження буде спрямовано на побудову оптимізаційних моделей на інших комбінаторних множинах з нелінійними функціями мети.

**Ключові слова:** інформаційна безпека, комбінаторна оптимізаційна модель, множина сполучень, цільова функція, обмеження.

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## ПРАКТИЧЕСКИЙ АСПЕКТ ПРИМЕНЕНИЯ КОМБИНАТОРНОЙ МОДЕЛИ НА КОНФИГУРАЦИИ СОЧЕТАНИЙ

**Введение.** На рынке программного обеспечения существует множество программных продуктов по защите информации. Выходя из основных задач о защите информации и финансовых возможностях, как правило, предприятию необходимо осуществлять выбор из имеющегося наличия программ данного типа. Выбор таких программ должен обеспечивать минимизацию затрат на их приобретение. При детализации выбора, можно произвести дополнительные расчеты целевой функции в диапазоне максимума и минимума среднестатистических цен программ по защите информации с учетом их рейтинга. При решении данной проблемы можно использовать комбинаторную оптимизационную модель на множестве сочетаний.

**Целью** данной статьи является демонстрация использования комбинаторной оптимизационной модели на множестве сочетаний и представления метода решения задач данного типа.

**Методы.** Метод решения задачи условной оптимизации на комбинаторном множестве сочетаний.

**Результаты.** Сформулирована проблема выбора программного обеспечения по защите информации и предложен подход к ее решению. В данном случае задача моделируется комбинаторной оптимизационной моделью на множестве сочетаний. Предложен метод решения задач данного типа. Рассмотрен практический пример применения комбинаторной оптимизационной модели на множестве сочетаний.

**Выводы.** С помощью предложенной модели можно моделировать задачи, которые предусматривают сочетание объектов, процессов и т.п. при условии минимизации функции цели. Дальнейшие исследования будут направлены на построение оптимизационных моделей на других комбинаторных множествах с нелинейными функциями цели.

**Ключевые слова:** информационная безопасность, комбинаторная оптимизационная модель, множество сочетаний, целевая функция, ограничения.